Catching-up and regulation in a two-sector Small Open Economy

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Abstract
Deregulation is often aimed at reducing mark-up pricing in technologically stagnant sheltered sectors. We show that this may decrease the process of catching-up and welfare since it shifts resources away from R&D-intensive tradables sectors. We analyse catching-up and deregulation in an R&D-based growth model that allows for international capital mobility, trade, and spillovers. Knowledge spillovers raise the productivity of R&D in the exposed sector which results into catching up. In the long run, the economy grows at the exogenous world growth rate. Capital mobility speeds up convergence. Temporary shocks have long-lasting effects as the economy exhibits hysteresis.

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1. Introduction

In neoclassical growth theory, emerging economies are characterized by a relatively low capital intensity. The scarcity of capital implies a high rate of return on investment and a corresponding high rate of growth. Alternatively, one could assume that emerging economies lack the knowledge to produce at the same level as developed economies. Knowledge can of course be imitated and the relevance of international knowledge spillovers is well documented (e.g. Coe and Helpman, 1995; Coe, Helpman and Hoffmaister, 1997). However, technological knowledge may be assumed to be firm-specific, at least to an important degree. This implies that knowledge spillovers have to be absorbed by own R&D outlays. Emerging economies may then be characterized by a technical disadvantage, which can be overcome by investing sufficiently in domestic R&D. Therefore, emerging economies may grow fast because there is potential for “catching-up”.

In this paper we analyse catching-up in the context of a small open economy with two sectors. The exposed or tradables sector consists of a number of specialized producers which have to compete in the international market by setting prices and investing in R&D. The economy is relatively backward because firms in the exposed sector stay behind in knowledge vis a vis the rest of the world. This implies two things. First, there is a potential for imitation. Second, investment in R&D in the emerging economy commands a relatively high rate of return. Both factors contribute to a rate of growth in excess of that in the rest of the world, so that the exposed sector catches up. There is no technological change in the sheltered or non-tradables sector, but workers in this sector benefit from growth in the exposed sector as the terms of trade move in favour of non-tradables (Balassa effect).

It is assumed that the sheltered sector is subject to a form of regulation that restricts the number of firms by preventing entry. Therefore, regulation gives room to oligopolistic price setting, allowing firms to set a mark-up over marginal cost. As a result, output in the sheltered sector is restricted. More resources are available for the exposed sector so that investment in R&D becomes more profitable. The implication is that regulation in the sheltered sector speeds up growth and may for that reason be seen as a kind of development strategy, be it deliberate or not. Whether it is also optimal from the point of consumer welfare remains to be seen.

An important aspect of the present analysis is the prevailing regime with respect to international capital mobility. We distinguish two extreme cases, i.e. balanced trade and perfect capital mobility. The results differ substantially among regimes. Under capital mobility, the relatively backward economy is able to smooth consumption by borrowing in the early stages of growth and by servicing the incurred debt later on. Long-run consumption will be lower than under the regime of balanced trade, which means that
less resources are needed to meet the demand for non-tradables. As a consequence, firm size in the tradables sector will be larger, which makes R&D more attractive. The economy catches up to higher levels of productivity, the more debt is accumulated, which in turn depends on the initial knowledge gap. This shows that hysteresis applies, not only with respect to foreign asset positions, but also with respect to the allocation of non-reproducible resources.

It may be useful to relate our analysis to the existing literature. The engine of growth applied in the present paper is borrowed from our earlier work on endogenous growth (Smulders and Van de Klundert, 1995; Van de Klundert en Smulders, 1997). There is a number of theoretical papers on catching-up driven by a knowledge gap but most papers assume that emerging economies learn from doing (e.g. Lucas, 1993; Maggi, 1993; Van de Klundert and Smulders, 1996; Basu and Weil, 1996). In the present model the backward economy has a substantial potential for investing in new knowledge. In Barro and Sala-i-Martin (1997) international diffusion of knowledge requires investment by the recipient country, but there is no international trade in the model. Two-sector open economies are analysed in Turnovsky and Sen (1991, 1995). The authors discuss changes in government expenditure and supply shocks in a neoclassical world with homogenous capital. As the regime of balanced trade is not analysed, it is not possible to isolate the implications of introducing perfect capital mobility in their model.

The paper is organised as follows. In Section 2 we present the model for the dependent economy and its behavioural implications. Section 3 is devoted to an analysis of the steady state characteristics of the system. Equilibrium dynamics are discussed in Section 4, applying a linearized version of the model. The dynamics in case of capital mobility turn out to be rather complicated. For this reason catching-up phenomena and regulation in the sheltered sector are discussed in more detail by presenting numerical examples in Section 5. The paper closes with some conclusions. Technicalities are relegated to a number of Appendices.

2. The dependent economy

Feasible growth
Preferences and technology are specified in Table A. Consumers trade off future consumption for present consumption according to an intertemporal utility function that features a constant elasticity of intertemporal substitution $1/\rho$ (assumed to be smaller than unity) and a pure rate of time preference $\hat{\rho}$, equation (A.1). They make a choice at every instant of time between non-tradables $Y_c$ and tradables $X_c$ according to the Cobb-Douglas specification in equation (A.2). The $X$-good in the consumption menu consists of a bundle of $N$ domestic goods and $n\tilde{N}$ foreign goods. Here $n$ stands for the number of
countries from which goods are imported. Variables with an upper bar relate to the outside world. The number of domestic and foreign varieties of $X$-goods is given. These goods are imperfect substitutes as shown in equation (A.3). The elasticity of substitution is constant and equals $\varepsilon > 1$.

Non-tradables are produced by applying labour with fixed productivity $h_Y$ as shown in equation (A.4). There is no technical change in the $Y$-goods sector. Goods in the tradables sector are produced by labour and intermediary inputs from the non-tradables sector with a Cobb-Douglas technology, equation (A.5). Factor productivity in each branch of the tradables sector can be improved by employing labour in R&D activities, as appears from equation (A.6). Innovation builds upon a knowledge base, which is the result of in-house or firm-specific knowledge accumulated in the past ($h_\alpha$) and of domestic spillovers as well as of foreign spillovers. These spillover effects are related to average knowledge levels at home ($H$) and abroad ($\bar{H}$). There are diminishing returns with respect to firm-specific knowledge ($0 < \alpha_0 + \alpha_f < 1$) but constant returns with respect to the knowledge base as a whole.

Labour market equilibrium implies that the amount of labour available ($L$) equals total labour demand, equation (A.7). Non-tradables are consumed or used as inputs in the production of tradables, equation (A.8). Tradables are consumed at home or exported as appears from equation (A.9). Trade with the outside world is governed by alternative assumptions with respect to international capital mobility. In equations (A.10) we consider two regimes. In case of current account equilibrium exports equals imports and the LHS of (A.10) equals zero. The other case considered is perfect international capital mobility, which allows the domestic economy to accumulate foreign assets, $A$, which bear a fixed rate of interest ($r^* = \bar{r}$). It should be observed that prices of domestic varieties of the X-good are not given. Each producer of $X$-goods holds a unique position in the world economy because he or she is the sole supplier of a product variety. Therefore prices of export goods or import-competing goods can be set in the domestic economy. Prices of imported goods are of course determined abroad.

Feasible growth paths satisfy equations (A.1) - (A.10). We assume that the domestic economy is small relative to the ROW. Hence, foreign variables are determined by foreign conditions only and can be considered as exogenous variables. Preferences as well as production technology and R&D technology in the ROW are the same as in the domestic economy. In addition, it will be assumed that the ROW exhibits steady state growth with $\frac{\bar{h}_0}{\bar{h}_f} = \bar{g}$ constant, and that all foreign firms are the same so that there is a single price of foreign tradables ($p_{xj} = p_x$, all $j$). By choice of numeraire, $p_x = 1$.

**Behaviour**

Consumers maximize the intemporal utility function in three stages subject to budget constraints. The three stage budgeting system is formulated in Table B. In the first stage,
each consumer decides on the path of aggregate consumption over time, taking into account the accumulation of financial assets $F$. The nominal interest rate $r$ is exogenous in case of perfect international capital mobility. Otherwise $r$ is determined endogenously by domestic savings and investment. The wage rate is denoted by $w$.

The second stage divides consumption over tradables and non-tradables. In the third stage, consumers decide about spending on the different varieties of the tradable good produced at home or produced abroad. The maximization procedure gives rise to the familiar Ramsey rule, equation (B.4) and demand equations for non-tradables (B.5), domestically produced tradables (B.6) and imported goods (B.7). The procedure also generates price indices for consumption (B.8) and tradables (B.9) in the domestic economy.

Producer behaviour is summarized in Table C. Demand for each product variety comes from domestic and from foreign consumers as shown in equation (C.2). Producers consider total consumer demand $X_C$ and $\bar{X}_C$ as well as the corresponding price indices $P_X$ and $\bar{P}_X$ as given. Profit maximization therefore results in a mark-up over marginal cost which is equal to the factor $\epsilon/(\epsilon - 1) = \mu_X$, equation (C.3). The cost-minimizing factor input combination follows from equation (C.4).

The optimal R&D-strategy implies that the marginal value product of labour employed in research $p_h \xi K_i$ should be equated to the marginal cost of labour $(w)$, as is shown in equation (C.5). The shadow price of the knowledge base $p_h$ is introduced as a Lagrangian multiplier in the maximization procedure. Firms face a trade-off with respect to investing in knowledge as appears from the no-arbitrage condition in equation (C.6). This condition says that investing a fixed amount of money in the capital market (the RHS of (C.6)) should yield the same revenue as investing that same amount of money in knowledge production. The latter raises factor productivity in commodity production and hence revenue [first term on the LHS of (C.6)], it raises also the knowledge base in R&D (second term) and it yields a capital gain (last term).

In the non-tradables sector, a regulated number of symmetric firms compete in homogenous markets. Competition a la Cournot prevails so that each firm takes as given total spending in his market as well as output of rival firms. Profit maximization results in the market price that is defined in equation (C.7), where $m$ is the number of homogenous and symmetric firms in the Y-sector. Regulation exogenously limits the number of firms $m$, for instance through a system of licences or permits. In the sequel we study changes in regulation that directly affect the number of firms in the non-tradables sector. This change affects the economy only through the resulting change in the mark-up rate. Hence, we capture changes in regulation by exogenous changes in the variable $\mu_Y$.

Throughout the paper we assume that also in the tradables sector firms are symmetric. Hence we drop all subscripts $i$ and $j$ (for all $i$ we have $h_{xi} = h_x, p_{xi} = p_x$, etc.).
3. The steady state

The model can be conveniently reduced to a number of key relationships. Appendix II derives six semi-reduced forms which can be interpreted as the savings decision, investment decision, labour market equilibrium, equilibrium in the markets for tradables and for non-tradables, balance of payment equilibrium and the balance of payment regime (see table F). As shown in Appendix III, the semi-reduced model easily reveals the steady state conditions which are further discussed in this section.

In the steady state, productivity levels in the domestic tradables sector grow at the same rate as abroad, i.e. at given rate \( \dot{g} \). The allocation of labour and the knowledge gap \( \dot{h}_x / \dot{h}_z \) are constant. The balanced growth path can be characterized as

\[
\frac{\dot{h}_x}{\dot{h}_z} = \frac{\dot{x}}{x} = \frac{\dot{X}_c}{X_c} = \frac{l}{\sigma C} = \frac{1}{1-\sigma} \frac{P_C}{w} = \frac{\dot{w}}{w} = \frac{\dot{A}}{A} = \frac{\dot{g}}{g}
\]

The price of imported goods is set equal to unity \( (p_x = 1) \). The steady state price of tradables should therefore be constant in the domestic economy \( (p_x = 0) \).

Table D displays five key relationships that hold in the steady state. Equations (D.1) - (D.5) can be used to find the steady state solutions in \( h_x \) and \( L_x \). Substitution of (D.1) in (D.2) results in a first equation in these variables. Substitution of \( CP_C / w \) according to equation (D.5) in (D.4) and substitution of the result in equation (D.3) gives the second equation in \( h_x \) and \( L_x \). From these equations we get:

\[
\frac{h_x}{h_z} = \left( \frac{\xi \beta}{\theta + [\sigma(\rho-1)+\alpha_h+\alpha_f+\beta]g} \right) \left[ \frac{L}{N} - \frac{A}{N} \frac{r-g}{w} \right] \left[ \frac{\sigma \mu}{\sigma(1-\gamma+\gamma \mu)_X} \right]^{1/\alpha_f} ,
\]

\[
L_x = \beta \gamma \left[ \frac{0}{\theta + [\sigma(\rho-1)+\alpha_h+\alpha_f+\beta]g} \right] \left[ \frac{L}{N} - \frac{A}{N} \frac{r-g}{w} \right] \left[ \frac{\sigma \mu}{\sigma(1-\gamma+\gamma \mu)_X} \right] ,
\]

where

\[
\beta = \frac{\sigma \mu \gamma}{(1-\sigma) \mu_X + \sigma(1-\gamma+\gamma \mu)} .
\]

In case of current account equilibrium or balanced trade the net foreign asset position equals zero \( (A = 0) \). In that case the sign of the partial derivations with respect to the parameters can easily be established

\[
\frac{\partial h_x}{\partial N} < 0, \quad \frac{\partial h_z}{\partial N} > 0, \quad \frac{\partial h_x}{\partial \xi} < 0, \quad \frac{\partial h_z}{\partial \xi} < 0, \quad \frac{\partial h_x}{\partial \rho} < 0, \quad \frac{\partial h_z}{\partial \rho} > 0, \quad \frac{\partial h_x}{\partial \sigma} < 0, \quad \frac{\partial h_z}{\partial \sigma} > 0,
\]

\[
\frac{\partial h_x}{\partial a_h} < 0, \quad \frac{\partial h_z}{\partial a_h} < 0, \quad \frac{\partial h_x}{\partial a_f} > 0, \quad \frac{\partial h_z}{\partial a_f} > 0, \quad \frac{\partial h_x}{\partial \mu} < 0, \quad \frac{\partial h_z}{\partial \mu} < 0; \quad \frac{\partial h_x}{\partial \mu_X} > 0, \quad \frac{\partial h_z}{\partial \mu_X} < 0 .
\]
An increase in the number of firms ($N$) or a fall in R&D efficiency ($\zeta$) leads to a lower productivity level in the exposed sector in relation to the productivity level abroad ($\tilde{h}_x$). The same result is obtained if the rate of time preference ($\tilde{\theta}$), the rate of risk aversion ($\rho$) or the share of income spend on tradables ($\sigma$) is raised. Spillover effects whether of domestic origin ($a_h$) or of foreign origin ($a_f$) have a negative impact on the knowledge gap. An increase in $\mu_x$, which can be associated with more regulation in the sheltered sector, has a positive effect on the productivity level in the exposed sector. It can be concluded that regulation in the sheltered sector helps to modernize the exposed sector.

On the other hand less intensive competition in the exposed sector leading to a higher mark-up factor ($\mu_x$) induces a lower productivity level.

The signs of the partial derivatives with respect to employment in the production of tradables ($L_x$) help in explaining the results with respect to changes in the level of knowledge in the domestic economy. An increase in $N$ reduces the size of firms in the exposed sector, which makes R&D less attractive. A rise in $\mu_x$ leads to a reduction in the production of tradables with a similar effect on R&D. A higher time preference, an increase in risk aversion or a shift in preferences towards tradables induces a higher consumption level. In this case labour is reallocated from R&D activities towards production of tradables as well as non-tradables. Higher spillover effects have a negative impact on the incentive to invest in R&D. As a result some labour in R&D laboratories becomes redundant so that a reallocation towards production in both sectors becomes necessary. More regulation in the sheltered sector sets labour free for production and R&D activities in the exposed sector. Finally, it should be noted that an increase in $\zeta$ has no effect on the allocation of labour. The rise in productivity comes entirely from the increase in R&D efficiency.

In case of perfect capital mobility the dependent economy may accumulate foreign assets. Equations (1) and (2) reveal that any level of foreign assets ($A/w$) can be maintained in a steady state if the long-run productivity gap and labour allocation take the appropriate value. Hence, there is a continuum of steady states. The impact of a change in real foreign assets on $h_x/\tilde{h}_x$ and $L_x$ can be found by differentiation of equations (1) and (2) with respect to the level of real foreign assets:

$$\frac{\partial L_x}{\partial N} < 0, \quad \frac{\partial L_x}{\partial \xi} = 0, \quad \frac{\partial L_x}{\partial \theta} > 0, \quad \frac{\partial L_x}{\partial \rho} > 0, \quad \frac{\partial L_x}{\partial \sigma} > 0, \quad \frac{\partial L_x}{\partial a_h} > 0, \quad \frac{\partial L_x}{\partial a_f} > 0, \quad \frac{\partial L_x}{\partial \mu_x} > 0, \quad \frac{\partial L_x}{\partial \mu_y} < 0.$$
An increase in foreign assets expressed in wage units raises capital income from abroad in real terms. Higher income boosts consumption and production of non-tradables, and crowds out domestic high-tech production and R&D. Lower investment in national research results in a larger productivity gap. Alternatively, one could say that there is a trade-off between the two assets, foreign claims and firm-specific knowledge.

The long-run equilibrium level of foreign assets is determined by history, i.e. the initial knowledge gap and all shocks during transition to the steady state. Perfect capital mobility gives rise to path-dependency, as will be shown in the next section.

4. Equilibrium dynamics

To study the dynamics it is convenient to linearize the model around the steady state. The key relationships in linearized form are given in Table E. Variables with a tilde relate to percentage deviations from their steady state solutions i.e. \( \tilde{x}(t) = dx(t)/x(t) \). Dependence on time index \( t \) is omitted where no confusion arises. The variable \( \tilde{a} \) is defined as the absolute deviation of \( A/h_x \) from its steady state solution, i.e. \( \tilde{a} = d(A/h_x) \). The linearization procedure is explained in Appendix IV.

**Balanced trade**

In case of equilibrium on the current account equation (E.6) can be simplified by setting \( \dot{\tilde{a}} = \ddot{\tilde{a}} = 0 \). The equations (E.1) - (E.6) can then be applied to derive a set of two linear differential equations in the level of knowledge (\( h_x \)) and production labour in the exposed sector (\( L_x \)). Equations (D.4) and (D.5) (which are valid also outside the steady state) can be used to arrive at

\[
\frac{Y_c}{h_x} = \frac{1-\sigma}{\sigma} \frac{\mu_x L_x}{\mu_Y Y}.
\]

Linearization of equation (3) implies

\[
\dot{\tilde{L}}_{yc} - \ddot{\tilde{h}}_{\gamma} = \dot{\tilde{L}}_{x} - \ddot{\tilde{\mu}}_{\gamma}.
\]

Substitution of equation (4) in equation (E.3) taking account of the definition of \( \beta \) results in the first differential equation:

\[
\dot{\tilde{h}}_x = -(\sigma, \beta) \tilde{h}_x - \left( \frac{\zeta L_x}{\beta_Y} \right) \frac{\eta_x}{1-\beta_Y} \frac{\bar{\mu}_Y}{\beta_Y}.
\]

Substitution of equation (4) in equation (E.5) gives an expression for \( C \) which can be
differentiated with respect to time. Applying equations (E.1) and (E.5) to eliminate the growth rate of consumption \( \dot{C} \) we arrive after some manipulation at

\[
\dot{L}_x \left( \frac{\rho(e-\sigma)+\sigma}{e} \right) = \left[ \beta + \alpha_h + \sigma(\rho-1)/\mu_x, \frac{\zeta L_x}{\beta Y} \right] \dot{L}_x - \alpha \left[ \beta + \left( \frac{\sigma(\rho-1)}{e} + \alpha_h \right) \right] \tilde{h}_x - \left[ \alpha_h + \sigma(\rho-1)/\mu_x, \frac{\zeta L_x(1-\beta Y)}{\beta Y} \right] \tilde{\mu}_Y. \tag{6}
\]

From equations (5) and (6) we see that the \( \dot{h}_x = 0 \) locus slopes downward and that the \( \dot{L}_x = 0 \) locus slopes upward. Moreover, it can be easily checked that the determinant of the matrix of coefficients with respect to \( h_x \) and \( L_x \) is negative. Therefore, the model is saddlepoint stable. The phase diagram is shown in the left panel of figure 1. The broken line represents stable arm of the saddlepath which is upward sloping as is illustrated in the figure. For an initial value of the level of knowledge, \( h_x(0) \), the amount of labour allocated to the production of tradables, \( L_x \), jumps to the stable arm. Thereafter both variables \( h_x \) and \( L_x \) adjust towards the steady state as indicated in the figure. The speed of adjustment is determined by the negative eigenvalue of the matrix of coefficients with respect to the state variables in equations (5) and (6).

More regulation in the sheltered sector goes along with an increase in \( \mu_r \). This leads to an upward shift of the stable arm of the saddlepath as shown in the right panel of figure 1. From equation (E.1) it appears that the rate of interest \( \tilde{r}(t) \) does not change in the long run, \( \tilde{r}(\infty) = 0 \). Substitution of this result in equation (E.2) gives:

\[
\dot{L}_x(\infty) = \alpha_f \tilde{h}_x(\infty). \tag{7}
\]

If the rate of interest is constant a rise in \( L_x \), inducing a higher rate of return on investment in R&D, has to be compensated by an increase in \( h_x \), which lowers productivity in the R&D department. Equation (7) leads to a proportional change of both variables along the ray OS in the right panel of figure 1. The new steady state is found at point \( S' \). On impact of the shock, \( L_x \) jumps towards the new stable arm. From there on the economy gradually approaches the new long-run equilibrium. More regulation in the sheltered sector increases prices of nontradables relative to importables. Imports rise and domestic production has to rise in order to pay for these imports. Hence \( L_x \) jumps up on impact. Larger sales stimulate incentives for innovation and firms increase R&D efforts. As productivity levels in the exposed sector rise faster, the price of domestic tradables declines and consumers shift their consumption further away from non-tradables. Whether it is optimal from a welfare point of view to increase \( \mu_r \) will be discussed in Section 4.

Perfect capital mobility

8
Under perfect international capital mobility the domestic rate of interest equals the foreign rate of interest which is constant. As a consequence: $\bar{r}=0$. Substitution of this result in equations (E.1) and (E.2) along with substitution of equation (E.5) in equation (E.3) results in a system of four differential equations in $C$, $h_x$, $L_x$, and $a$. In the steady state $\dot{C} = \dot{h}_x = \dot{L}_x = \dot{a} = 0$, but that leaves us with three equations in four unknowns, because equation (E.1) with $\bar{r}=0$ is always satisfied. This implies that the model exhibits hysteresis: we need to know the entire transition dynamics to solve for the steady state.\(^3\)

The information contained in equation (E.1) can be preserved by integration of this equation which yields:

$$\dot{C} = \dot{h}_x = \dot{L}_x = \dot{a} = 0,$$

where $v$ is the constant of integration, which can be interpreted as the permanent change in consumption (due to a shock that hits the economy) for given values of $h_x$ and $L_x$. Access to the international borrowing at a given rate allows for consumption smoothing in response to shocks. A shock that increases the ex-ante domestic rate of return above the international interest rate will induce borrowing in the international market at the cost of incurring a debt and the associated long-run interest burden. In this case, the long-run permanent change in consumption is negative. Indeed, in general, the permanent consumption change, or wealth effect, $v$, crucially depends on the size of the shock and on its impact on the development of the ex-ante domestic rate of return over time.

Equation (8) can be used to eliminate $L_x$ from the equations in Table E. The variable $\dot{L}_x$ can be eliminate by using equation (E.1). As shown in Appendix V, the model can be reduced to a system of differential equations in three state variables, which can be written in matrix notation as:

$$\begin{bmatrix}
\dot{h}_x \\
\dot{C} \\
\dot{a}
\end{bmatrix} = \begin{bmatrix}
a_{11} & a_{12} & 0 \\
a_{21} & a_{22} & 0 \\
a_{31} & a_{32} & r-g
\end{bmatrix} \begin{bmatrix}
\dot{h}_x \\
\dot{C} \\
\dot{a}
\end{bmatrix} + \begin{bmatrix}
a_{14} & \left(1-\sigma\right) & 0 \\
a_{24} & \left(1-\sigma\right) & 0 \\
a_{34} & -a_{34} & a_{36}
\end{bmatrix} \begin{bmatrix}
\bar{r} \\
\bar{h}_y \\
\bar{a}
\end{bmatrix} = \begin{bmatrix}
\bar{v} \\
\bar{v} \\
\bar{v}
\end{bmatrix} \quad \text{(10)}$$

As explained in Appendix V the permanent consumption effect $\bar{v}$ can be found along with the time paths of $\bar{h}_x$, $C$ and $\bar{a}$ by imposing solvability with respect to the net foreign position and assuming $\bar{a}(0)=0$. Moreover, it is shown there that the dynamics of the model can be represented by a phase diagram in $\bar{h}_x$ and $C$. The slope of the stable manifold depends on the intensity of foreign spillovers and the elasticity of demand $\epsilon$. For $\alpha_f$ larger (smaller) than $\epsilon-1$ consumption and productivity change in the same (opposite) direction along the transition path. The intuition behind this result is given
below. The relation between net foreign assets \((a)\) and productivity \((h_x)\) is negative. Intuitively, investment in domestic knowledge and investment in foreign assets are substitutes. The two-panel diagrams in figure 2 depict the relations among the three state variables \(h_x\), \(C\), and \(a\) for a large and a small value of \(\alpha_f\) respectively. The broken curve in both figures indicates the stable arm of the saddlepath with respect to \(h_x\) and \(C\).

In order to gain some insight in the time path of consumption, we combine equations (7) and (8), which results in:

\[
\hat{C}(0) - \hat{C}(\infty) = \frac{1-\sigma}{\rho \varepsilon} \left[ (\varepsilon - 1 - \alpha_f) \hat{h}_x(\infty) + \hat{L}_x(0) \right].
\]

The initial jump in high-tech employment \((L_x)\) can be derived from (E.2)* and substituted into (9), which yields:

\[
\hat{C}(0) - \hat{C}(\infty) = \frac{1-\sigma}{\rho} \left[ \eta \alpha_h + (1-\eta) \left( \frac{\varepsilon - 1 - \alpha_f}{\varepsilon} \right) \hat{h}_x(\infty) \right],
\]

where \(\eta = -\lambda/[\varepsilon(\zeta L_x/\gamma) - \lambda]\) and \(\lambda < 0\) is the stable root of the dynamic model.

Equation (11) shows that the timing of consumption depends crucially on the balance between the elasticity of demand for exportables \(\varepsilon\) and spillover parameters. If \(\alpha_f\) is small relative to \(\varepsilon - 1\), consumption grows less over time, i.e. \(C(0) > C(\infty)\). In other words, consumers wait to save and draw a bill on the future. The reason is that consumer prices tend to rise over time. Note that only prices of nontradables matter for the consumer price index, since the share of home-produced tradables in total tradables consumption of the small open economy is negligible. Prices of non-tradables depend on wage costs. Higher productivity in the exposed sector drives up wage costs for the sheltered sector. Price increases in this sector fuel consumer price inflation\(^5\) which makes it attractive to consume now rather than in future. However, if \(\alpha_f\) is large, a counterforce becomes important. Employment and production in the tradables sector will increase substantially in response to productivity changes (see (7)), which lowers the price of tradables. Consequently, wage costs fall, and the consumer price index falls. Note that the price fall in response to a productivity improvement is steeper the lower the price elasticity \(\varepsilon\) is. Hence, if \(\alpha_f\) is large relative to \(\varepsilon\), consumption levels will rise over time (more than in the initial steady state), and if \(\alpha_f\) is small relative to \(\varepsilon\), consumption will rise less over time.

The effects of an increase in \(\mu_r\) are illustrated in figure 3 for the case \(\alpha_f > \varepsilon - 1\). The \(\hat{h}_x = 0\) locus shifts upward and the \(\hat{C} = 0\) locus shifts downward. These shifts imply a downward movement of the stable arm of the saddlepath. On impact of the shock consumption declines, but as productivity in the exposed sector improves consumption goes up again. The amount of foreign assets declines, because consumers incur foreign debt to smooth consumption over time.\(^6\)
The picture shown in figure 3 is merely an illustration, because the shift of the $\dot{h}_s = 0$ locus and the $\dot{C} = 0$ locus cannot be analytically determined in a meaningful way. To get a better understanding of the implications of a change in $\mu_Y$ numerical examples may therefore be useful.

5. Numerical examples

Although in case of balanced trade the model can be solved analytically it is instructive to compare numerical results under both regimes with respect of the balance of payments. The parameter values for the reference path are equal to:

$$
\begin{align*}
\rho &= 2, \quad \hat{\rho} = 0.03, \quad \sigma = 0.8, \quad \varepsilon = 2.5, \quad \alpha_h = 0.5, \quad \alpha_r = 0.4, \quad \xi = 0.01, \quad \gamma = 0.8, \quad \mu_Y = 1.1, \quad h_s = 1, \quad L = 82.4, \\
n &= 25, \quad N = \bar{N} = 8, \quad g = 1.877\%.
\end{align*}
$$

In the reference path, net foreign assets are zero. The calculations presented for both regimes are percentage deviations from this reference path. Because the time paths of the variables are monotonic it is sufficient to present results for the periods $t=0$ and $t=\infty$.

Catching-up

Catching-up occurs when the level of knowledge in relation to the foreign level lies below the steady state values. In a linearized version of the model this boils down to a negative deviation of $h/h_s$ from its (future) steady state level. The outcomes in case the initial level of knowledge in the domestic economy lies 1% below its steady state value under balanced trade are given in Table 1.

Under balanced trade the system converges to a unique steady state. Catching-up implies a rise in the knowledge level and a temporary higher rate of growth of total factor productivity in the exposed sector. As a result of this process consumption of tradables and non-tradables rises. The initial rate of interest lies above the world level. This makes it attractive for firms to employ a large share of employment in R&D initially. As the level of knowledge approaches its steady state level the rate of interest converges towards the level prevailing in the rest of the world. In the steady state both rates of interest should be equal because the rates of growth are then equal and consumer preference are assumed to be the same everywhere, equation (D.1).

In case of perfect international capital mobility there is an inflow of foreign capital to equate interest rates in every period. Consumers as a group are in a position to borrow abroad in order to smooth consumption over time. The preference for current consumption implies that consumption declines over time in contrast with the case of balanced trade. In the long run consumers have to service foreign debt, incurred in the
course of the transition to a new steady state. Long-run consumption is lower than under balanced trade. Therefore, less labour needs to be allocated to produce non-tradable consumption goods. More labour is allocated to tradables production which increases firm size. R&D becomes more attractive and the level of productivity rises above to steady state level attained under balanced trade ($\bar{y}(\infty)>0$).

There is no unique steady state solution under capital mobility for a given set of structural parameters. If the economy starts at a level of knowledge which is 2% below the value attained in the steady state under balanced trade, all results for $t = \infty$ in case of capital mobility double. Therefore, productivity levels are path-dependent and convergence of countries in terms of productivity levels depends on initial positions. This result flies in the face of the standard views on convergence in neoclassical theory. Moreover, most of this literature is based on the notion of a closed economy (e.g. Barro and Sala-i-Martin, 1995). If capital mobility is assumed in a neoclassical context the economy jumps instantaneously to its unique steady state levels. Physical capital is imported so as to equate the marginal product of capital with the going rate of interest on world capital markets. Partial international mobility of capital in the sense that physical capital can be used as collateral for international borrowing, but human capital cannot gives standard neoclassical results with the economy adjusting gradually to its unique long-run equilibrium (cf. Barro, Mankiw, Sala-i-Martin 1995).

Path-dependency of consumption levels is a well-known feature of small open economies. In response to adverse temporary domestic shocks, foreign borrowing allows consumers to mitigate the short-run fall in consumption, at the cost of higher debt service and lower long-run consumption. In a one-sector economy, the accumulation of capital is not affected as long as the supply of other factors of production (labour) remains the same so that the physical marginal productivity of capital is not affected (cf. Blanchard and Fisher, 1989, p.66). However, if the path-dependent change in consumption affects both tradable and non-tradable production, as in our model, the allocation of labour over the two sectors is permanently affected. Then also the incentives to accumulate capital in the different sectors of the economy are permanently affected which results in a long-run change in the domestic capital stock (see in this connection also Turnovsky and Sen, 1991 and 1995).

*Increasing regulation*

Table 2 presents the results of a one percent permanent rise in $\mu_y$. This corresponds to a change in regulation such that a smaller number of firms is allowed to operate in the non-tradable sector. An increase of the mark-up factor in the sheltered sector induces a fall in output and employment on impact of the shock. Labour is relocated from the sheltered to the exposed sector so that R&D becomes more attractive.

Under balanced trade the interest rate rises to generate the necessary savings. This
implies that the level of consumption declines in the short run. Productivity in the tradables sector rises over time. The additional products can be sold, because the rise in productivity allows for a reduction in prices. The increase in knowledge reduces the rate of return on investment and in the long run the rate of interest falls back to its original level as does the rate of growth. However, the long-run consumption level increases because of a rise in productivity in the exposed sector.

In case of capital mobility consumption goes up in the short run and the economy runs a balance of trade deficit. The inflow of capital is sufficient to keep the rate of interest at the level in the outside world. Compared with the case of balanced trade there is now less need to increase the production of tradables at \( t = 0 \). As a consequence there is more labour available for R&D activities and the level of productivity in the exposed sector rises faster than under balanced trade as appears from the rate of growth. The increase in foreign debt induces a burden in the long run. In the new steady state the economy must run a trade surplus to service debt. Compared with the balanced trade regime, long-run consumption both of tradables and non-tradables is lower, while productivity in the exposed sector is higher.

Despite increased regulation, intertemporal welfare (calculated at time zero) rises under both regimes. Whether this conclusion is robust will be investigated below.

**Welfare considerations.** Changes in welfare depend on the initial value of \( \mu_y \). This can be shown by a sensitivity analysis with respect to the mark-up factor in the sheltered sectors in the initial steady state. Figure 4 presents the results. On the horizontal axis is the initial value of \( \mu_y \). On the vertical axis is the change in intertemporal welfare as a result of a small increase in \( \mu_y \). Welfare is the present discounted value of consumption as of the period of the policy shock. The optimal value \( \mu_y^* \) for which the change in welfare equals zero is above unity in both balance of payment regimes.

Optimal mark-up rates are lower than in a closed economy without growth where welfare is not distorted if mark-up rates are equal across sectors. This would imply \( \mu_y^* = \mu_x = \varepsilon / (\varepsilon - 1) = 1.67 \) in this example. In the open economy, a rise in \( \mu_y \) induces an expansion of the tradables sector and a loss in the terms of trade as more goods have to be sold abroad. Therefore the optimal mark-up rate in the non-tradables sector has to be lower than the mark-up rate prevailing in the tradables sector. Indeed, it can be proven that a value of \( \mu_y \) that equals \( \mu_x (\varepsilon - 1) / \varepsilon = (1) \) maximizes national welfare of the small open economy without growth by optimally trading off terms of trade gains and domestic price distortions.\(^8\)

Next, growth effects should be taken into account in the determination of the welfare maximizing value of \( \mu_y \). Because of knowledge spillovers, high-tech firms invest too little in R&D. When \( \mu_y \) is raised, demand for high-tech products increases which boosts the rate of return to innovation. Hence, higher mark-ups in the sheltered sector
provide a second-best instrument to compensate the dynamic distortion in the exposed sector.⁹

Finally, the balance of payment regime plays a role. Capital mobility provides an additional reason to regulate the sheltered sector. Under capital mobility, regulating the sheltered sector is a more efficient instrument to compensate the knowledge externality than under balanced trade so that the optimal $\mu_\gamma$ is larger under the former regime than under the latter one. Stimulating investment is less costly when the supply of foreign savings is perfectly elastic. In contrast, when trade has to be balanced, increasing $\mu_\gamma$ result in temporarily high rates of interest which impose an intertemporal welfare cost. In the absence of national knowledge spillovers ($\alpha_n=0$), both regimes call for zero regulation ($\mu_\gamma=1$).¹⁰

Excessive regulation (policies that set $\mu_\gamma$ above $\mu_\gamma^*$) bring about welfare losses. Figure 4 shows that the welfare losses are smaller in the regime of capital mobility than in the regime of balanced trade if regulation is modest. However, if the sheltered sector is heavily regulated, balanced trade performs better. First note that under capital mobility, the optimal level of regulation is higher, so that starting from modestly high $\mu_\gamma$ society still reaps welfare gains by regulating under capital mobility, while under balanced trade it incurs losses. However, note also that welfare is more sensitive to regulation under capital mobility than under balanced trade (compare the slope of the two curves in figure 4). Supply of funds is perfectly elastic which allows investment to be more sensitive to changes in innovation incentives. Excess regulation creates overaccumulation of the national knowledge stock and expansion of tradables that is larger than under balanced trade. The associated larger deterioration in the terms of trade makes capital mobility perform worse.

X-inefficiency. Returning to regulation, it is often argued that regulation in the sheltered sector induces X-inefficiency. In our model a change in X-inefficiency can be introduced in the form of an autonomous change of labour productivity in the sheltered sector ($h_\gamma$). A rise in $h_\gamma$ leads to an immediate decline in consumption levels, but has no effect on the accumulation of knowledge. This can easily be checked in case of balanced trade. Inspection of the equations (5) and (6) reveals that there is no term in $h_\gamma$. A similar result holds in case of capital mobility as appears from numerical simulation of the system of equations in (10). Intuitively, a decline in output of non-tradables caused by a fall in labour productivity induces a proportional increase in the price of these goods. This induces a proportional decline of the demand for non-tradables. This implies that there is no need for a reallocation of labour. Consumption of tradables also declines, because producers apply less non-tradables in the production process. The welfare consequences of induced X-inefficiency, if any, have to be taken into account in a final assessment of regulation in the sheltered section.
6. Conclusions

Emerging economies are able to catch up by investing in R&D. The larger the knowledge gap, the higher the rate of return and the faster growth. The international capital market can boost convergence because additional investment can be financed without inducing a rise in the interest rate. This allows consumers to take an advance on future welfare by smoothing consumption over time.

Under capital mobility, temporary country-specific shocks have permanent effects on net foreign asset positions and productivity (hysteresis). Hence, countries that are symmetric in economic structure and in technological and social capability may hold different net foreign asset positions which result in different total factor productivity levels. This may explain for the lack of productivity convergence in exposed sectors of the economy (cf. Bernard and Jones 1996).

In developing countries, the sheltered sector may be operating on the basis of traditional rules and norms. As a result, the absence of perfectly competitive markets may cause mark-up rates in this sector. Deregulation would lower markup rates. However, national economic policies that deliberately abstain from reducing high markup rates in the sheltered sector of the economy may boost national productivity growth. Such a strategy may offset dynamic distortions in the economy because of knowledge spillovers, so that regulation in the sheltered sector may improve welfare.

However, when markup rates in the sheltered sector become too large, welfare losses will occur. Productivity growth in the dynamic exposed sector of the economy will be high, but at the cost of severe price distortions. Capital flows will exacerbate the overaccumulation of capital, so that welfare losses are larger under capital mobility than under balanced trade. International capital mobility aggravates policy mistakes. National policy authorities may therefore adopt capital flow restrictions in small open economies in order to mitigate the adverse welfare effects of mistakes in regulation.

References
Endnotes

1. Financial assets \((F)\) include shares issued by domestic firms, domestic consumer loans and foreign assets \((A)\). Firms’ profits accrue to the holders of the first type of assets. Firms in the tradables sector have to issue new shares to finance R&D investments. In the absence of capital mobility foreign assets are equal to zero \((A=0)\). Note that we restrict the analysis to a perfect capital market in which the rate of return to any of the assets to which the investor has access bears the same rate of interest.

2. The non-tradables sector can be thought of as being subdivided in a large number of symmetric subsectors in each of which a small number \((m)\) of homogenous producers that compete \textit{a la} Cournot.

3. A steady state arises only if foreign and domestic rates of time preference \((\bar{\theta})\) are equal. We have assumed that both are exogenous and we imposed equality. Alternatively, the domestic rate of time preference may be endogenous along the lines of Uzawa (1968). If \(\bar{\theta}\) changes in response to other variables of the model, these changes will be reflected in eq. \((E.1)\) so that this equation can be used to determine the steady state. Accordingly, the multiplicity of steady states vanishes. Two problems, however, arise. First, the well-known objection against the Uzawa formulation applies, viz. for stability reasons, \(\bar{\theta}\) should be increasing in utility which seems difficult to defend a priori (Blanchard and Fisher 1989, p.73). Second, Uzawa analysed the case that the rate of time preference depends on utility in a model without long-run growth. In our model long-run utility is growing so that no steady state arises if \(\bar{\theta}\) depends on utility.

4. Note that if the stable root of the dynamic model equals \(\lambda\), for any variable \(x\) we may write \(\dot{x}(t) = \lambda [x(t) - x(\infty)]\). Using this result to eliminate \(\dot{h}_x\) and \(\dot{L}_x\) in \((E.4)\), and subsequently substituting \(\bar{r}=0\), \(h_x(0)=0\) and equation \((7)\), we find \(L_x(0)=\eta[\varepsilon\alpha_x-(\varepsilon-1-\alpha_y)]h_x(\infty)\), where \(\eta\) is defined as in the main text.

5. This can be clearly seen by inspecting equations \((AA.14)-(AA.16)\) in the Appendix.

6. The stable arm of the saddle path shown in the lower panel of figure 3 does not shift, because \(\tilde{a}(0)=0\). See also Turnovsky and Sen (1991).

7. In our numerical example, the rest of the world is characterized by exactly the same parameters as the domestic economy. Hence, we linearize around a steady state with \(h_x/h_x=1\). Note that by setting \(h_x/h_x=1\) and \(A=0\) in equation \((1)\), we find \(g_x\). The ROW can be considered as a closed economy with endogenous growth as in Smulders and van de

8. This result only holds if the share of domestically produced tradables is negligible in total consumption ($s \to 0$), which is the natural assumption if the country is really small and there is no "home-preference". With a larger share, we have $\mu_Y^{*} > 1$: production of tradables should be stimulated and their price should be lower, since prices of tradables now influence consumer prices. Intuitively, the larger $s$, the more we move to the closed economy case and the closer $\mu_Y^{*}$ will be to $\mu_Y$.

9. Only domestic spillovers matter in this respect. Foreign spillovers provide a flow of knowledge like manna from heaven. From a national perspective, no policy can influence this so it is not an externality that a small open economy can internalize.

10. Provided again that $s \to 0$. 
Appendix I. Solving for Price Variables

With symmetric firms within the country, all domestic firms charge the same price and consumption levels of any good from a certain country are the same. The foreign price of high-tech goods is taken as the numeraire. Hence, \( p_{xi} = p_x \) for all \( i \), \( x_{ci} = x_c \) for all \( i \), \( p_{ij} = 1 \) for all \( j \) and all \( t \). The value share of home-produced high-tech goods in total high-tech consumption, \( s \), can be found from (B.6) and (B.7):

\[
s = \frac{N_{x_i}p_x}{N_{x_i}p_x + n N x_c \bar{p}_x} = \frac{1}{1 + (nN/N)p_x^{t-1}}. \tag{Ap.1}
\]

The small open economy assumption implies that \( N \) is negligible relative to \( nN \) so that \( s \rightarrow 0 \). Hence, the consumer price index \( P_C \) depends on \( P_Y \) and \( p_x \) only. We find an expression for \( P_Y \) by eliminating \( w \) between (C.7) and (C.5):

\[
P_Y = \left( \frac{p_x h_x}{\mu_x} \right) \left( \frac{\mu_y}{h_y} \right)^\gamma \gamma^{-1}(1-\gamma)^{1-1}. \tag{Ap.2}
\]

From (B.8), (Ap.2), the small country assumption \( (s \rightarrow 0) \), and the choice of numeraire \( (\bar{p}=1 \text{ for all } t) \), we find, using hats to denote growth rates:

\[
\hat{P}_C = (1-\sigma)(\hat{h}_x + \hat{p}_x). \tag{Ap.3}
\]

We assume that preferences are equal and homothetic across the world. This means that any pair of goods is consumed everywhere in the same ratio as it is produced:

\[
x_{c_i}/\bar{x}_c = x_{c_i}/\bar{x}_c = x/\bar{x} = p_x^{-e}. \tag{Ap.4}
\]

where the last equality follows from (B.6) and (B.7).

Combining (A.5), (C.4) and (C.7), we find:

\[
x = h_x L_x \left[ \frac{h_y (1-\gamma) / \gamma \mu_y}{\mu_y / h_y} \right]^{-\gamma}, \tag{Ap.5}
\]

which holds also for foreign variables. Substitution of (Ap.5) in (Ap.4) gives:

\[
p_x = \left( \frac{h_x L_x}{h_x L_x} \right)^{-1/e} \left( \frac{\mu_y / h_y}{\mu_y / h_y} \right)^{(1-\gamma)e}, \tag{Ap.6}
\]

\[
\hat{p}_x = (\bar{g} - \bar{h}_x - \bar{L}_x)/\epsilon. \tag{Ap.7}
\]

where we have assumed that balanced growth prevails in the rest of the world so that \( \bar{L}_x \).
is constant.

**Appendix II. Key relationships**

Table F contains seven key relationships of the model in the variables $C$, $r$, $h_x$, $L_x$, $Y_c$, $p_x$, $P_C$, $w$, and $A$. This section of the appendix explains how to derive these semi-reduced forms. In the next sections of the appendix, we use the results, first, to characterize the steady state, and, second, to linearize the model and study the dynamics.

We derive the Ramsey equation in (F.1) by combining (B.4), (Ap.3) and (Ap.7).

The equation that characterizes the investment decision is found by substituting the appropriate equations in equation (C.6). First, divide the equation by $p_{hi}$. Eliminate $x$, $p_x$ and $p_{hi}$ in the first term by substituting (C.3), (Ap.5) and (C.5) respectively. Eliminate $L_i$ in the second term by substituting (A.6). The rate of change of the price of knowledge that appears in third term can be rewritten as $p_{hi} = p_{hi} + \alpha(h_x - \bar{g})$ by differentiating (C.5) with respect to time, taking into account that $h_x = H$, and using (C.3) and (C.7) to eliminate $\dot{w}$. We find (F.2) when we finally substitute (Ap.7) to eliminate $\dot{p}_x$ and introduce the definition

$$\zeta = \frac{\xi K_x}{h_x} = \xi \left(\frac{h_x}{\bar{h}_x}\right)^{\gamma_f}, \quad \text{(Ap.8)}$$

where the last equality follows from the symmetry assumption.

The labour market equation in (F.3) is derived as follows. From equations (C.4) and (C.7), we find

$$NY_x/h_y = (1 - \gamma)NL_x/\gamma \mu_y \quad \text{(Ap.9)}$$

Substituting (A.4), (A.8), (Ap.8) and (Ap.9) into (A.7), we find (F.3).

Equation (F.4) replicates (Ap.6). Equation (F.5) is found by combination of equations (B.5), (C.7) and (A.4).

In order to find the Balance of Payments equation, we substitute (B.3), (B.2) and (B.5) into (A.10), take into account symmetry, and find:

$$Nxp_x - \sigma CP_c = \dot{A} - \bar{r} A \quad \text{(Ap.10)}$$

Eliminating $x$ and $p_x$, by substituting (Ap.5) and (C.3) respectively, we arrive (F.6).
Appendix III. Steady State (Table D)

The steady state is characterized (defined) by constant growth rates. Equation (F.3) implies that \( L_x, Y_c \) and \( h/h_x \) should be constant. It can be checked from (F.5) and (F.6) that \( A/w \) should be constant. Hence, in the steady state we may write:

\[
\dot{L}_x = \dot{Y}_c = 0, \quad \dot{h}_x = \ddot{h}_x = \ddot{g}, \quad \dot{A} = \ddot{w} .
\] (Ap.11)

Then it follows from (F.4) and from (Ap.3), (Ap.5), (Ap.2), (C.7), and (F.5) respectively that:

\[
\dot{p}_x = 0 \quad \text{(Ap.12)}
\]

\[
\ddot{g} = \ddot{P}_c/(1-\sigma) = \ddot{x} = \ddot{P}_r = \ddot{w} = \ddot{C}/\sigma \quad \text{(Ap.13)}
\]

Substituting (Ap.11)-(Ap.13) into the key relationships in table F, we find their steady state counterparts which are displayed in table D in the main text.

Appendix IV. Linearization of the model (Table E)

The purpose of this section is to find the linearized version of the model in terms of the four main variables, viz. \( h_x, L_x, c, \) and \( a \), and three variables of secondary interest, viz. \( p, r, Y_c \). We introduce the variable \( a=A/h_x p_x \) (which equals \( a=A/h_x \) by our choice of the numeraire) which should be interpreted as the ratio of net foreign assets to domestic assets. We choose this variable because it is a predetermined variable (note that the ratio \( A/w \) which is used in section 3 is not), which allows us to exploit the condition \( da(0)=\ddot{a}(0)=0 \). Our linearization procedure involves taking total differentiation, where all parameters except \( \mu_r \) and \( h_x \) are considered as constants. Tilded variables are expressed as relative deviations from the initial balanced growth path, i.e. for any variable \( u, \ddot{u}=du/u \) or \( du=uu\ddot{u} \), so that \( da=\ddot{a} \). An exception is \( \ddot{a} \) which is defined as the absolute (rather than relative) deviation from the original growth path, i.e. \( a=da \) and \( d\dot{a}=\dot{a} \), which allows us to consider the situation in which \( A=a=0 \) initially (balanced trade).

Equations (E.1)-(E.4) directly follow from linearization of equations (F.1), (F.2), (F.3) and (F.4). In order to find equation (E.5), we first linearize (F.5). The resulting equation contains terms with \( P_c w \), which we want to eliminate. In order to find an expression for \( P_c w \), first note from (B.8), (B.9), the symmetry assumption, the small country assumption \( (s-0) \), and the choice of the numerair \( (p_x=1) \) that:
\[ \hat{P}_c = (1-\sigma)\hat{P}_r. \]  

(Ap.14)

Linearization of (C.7) and (C.3) gives:

\[ \hat{w} = \hat{h}_x + \hat{p}_x - (1-\gamma)(\hat{p}_r - \hat{h}_r). \]  

(Ap.15)

\[ \hat{p}_r = \hat{w} + \hat{p}_r - \hat{h}_r. \]  

(Ap.16)

Linearizing (F.5) and substituting (Ap.14), (Ap.15), (Ap.16) and (E.4), we find (E.5).

In order to find a convenient Balance-of-Payments relationship, we divide (F.5) by \( \hat{h}_x \) and rewrite the equation in terms of \( a = A/\hat{h}_x \) instead of \( A \):

\[ Nxp_x/\hat{h}_x - \sigma Cp_c/\hat{h}_x = \dot{a} + \tilde{g}a - \tilde{r}a. \]

Linearizing this expression (recalling our definition \( \tilde{a} = \Delta a \)), substituting (Ap.14), (Ap.15), and (Ap.16) to eliminate \( \tilde{P}c \) and \( \tilde{w} \), and substituting (E.4), we arrive at (E.6).

The six equations (E.1)-(E.6) contain seven variables (viz. \( \tilde{w}, \tilde{r}, \tilde{C}, \tilde{L}_x, \tilde{h}_x, \tilde{Y}_c, \tilde{a} \)). The equation that completes the system depends on which of the two Balance-of-Payments regimes applies. (E.7) summarizes the two regimes.

Appendix V. Solving the dynamics under Perfect capital Mobility

Representation of the model by three differential equations

Substitution of (E.5) and (E.7b) into (E.1)-(E.3) and (E.6) yields a system of four differential equations in the variables \( \tilde{c}, \tilde{L}_x, \tilde{h}_x, \) and \( \tilde{a} \). As explained in the main text, the dynamic system exhibits hysteresis and we need to further reduce the system. To this end we take the integral of (E.1) with \( \tilde{r} = 0 \). It gives the expression that allows to eliminate \( L_x \):

\[ \dot{\tilde{L}}_x = \left[ p(1-\sigma)/(1-\sigma) \right] (\tilde{C} - \tilde{v}) + (\epsilon - 1)\tilde{h}_x. \]  

(Ap.17)

where \( \tilde{v} \) is the constant of integration. Using this result to eliminate \( L_x \) and \( \dot{\tilde{L}}_x \) in (E.32), we find (for \( \tilde{r} = 0 \)):

\[ \dot{\tilde{C}} = \left( \frac{\zeta L_x}{\gamma} \right) \left[ \epsilon (\tilde{C} - \tilde{v}) + \left( \frac{(1-\alpha)(\epsilon - 1 - \sigma \rho)}{\rho} \right) \tilde{h}_x \right] - \frac{\alpha \left( 1 - \sigma \right)}{\rho} \tilde{h}_x. \]  

(Ap.18)

The elimination of \( \tilde{Y}_c \) between (E.3) and (E.5) and substitution of (Ap.17) in the resulting
-expression gives the expression for $\dot{h}_x$. Since we want to compare the regime of perfect
capital mobility to that of balanced trade, we linearize around an initial steady state
without net foreign assets. Hence we may substitute equation (3) from the main text. The
resulting expression is displayed in the matrix in (10) in the main text. The coefficients
are defined as:

$$a_{11} = -\left(\frac{\zeta L_x}{\gamma}\right)\left(\frac{1-\gamma+\gamma\mu_Y}{\mu_Y}\right)(e-1) - \alpha_p g$$  

$<0$

$$a_{12} = -\left(\frac{\zeta L_x}{\gamma}\right)\left[\left(\frac{1-\gamma+\gamma\mu_Y}{\mu_Y}\right)\frac{\rho}{1-\sigma} + \left(\frac{1-\sigma}{\sigma}\right)\frac{\mu_X}{\mu_Y}\left(\frac{\sigma\rho + 1 - \sigma}{1-\sigma}\right)\right]$$  

$<0$

$$a_{16} = \left(\frac{\zeta L_x}{\gamma}\right)\left[\left(\frac{1-\gamma+\gamma\mu_Y}{\mu_Y}\right)\frac{\rho}{1-\sigma} + \left(\frac{1-\sigma}{\sigma}\right)\frac{\mu_X}{\mu_Y}\left(\frac{\sigma\rho}{1-\sigma}\right)\right]$$  

$>0$

$$a_{14} = \left(\frac{\zeta L_x}{\gamma}\right)\left(\frac{(1-\sigma)\mu_X + \sigma(1-\gamma)}{\mu_Y}\right)$$  

$>0$

$$a_{21} = -\alpha_p a_{11}(1-\sigma)/\rho + (\zeta L_x/\gamma)(e-1-\alpha_p)(1-\sigma)/\rho$$  

$>$

$$a_{22} = -\alpha_p a_{12}(1-\sigma)/\rho + (\zeta L_x/\gamma)e$$  

$>0$

$$a_{24} = -\alpha_p a_{14}(1-\sigma)/\rho$$  

$<$

$$a_{31} = (N\sigma p/h_x)(e-1)$$  

$>0$

$$a_{32} = (N\sigma p/h_x)[\rho(\mu_Xe - \sigma)/(1-\sigma) - 1]$$  

$>0$

$$a_{36} = -(N\sigma p/h_x)\rho(\mu_Xe - \sigma)/(1-\sigma)$$  

$<$

$$a_{34} = -(N\sigma p/h_x)\left[(1-\sigma)\mu_X + \sigma(1-\gamma)/\mu_X\right]$$  

$<$
Finally we derive a differential equation for net foreign assets \( a \). Use (Ap.17) to eliminate \( L_x \) in (E.6). Under the condition of zero initial net foreign assets, this gives the third differential equation in (10).

Solving the dynamic system

From (10) and the initial conditions for the predetermined variables \( h_x \) and \( a \) we have to solve the time paths of \( \dot{h}_x, \dot{c}, \) and \( \dot{a} \), and the unknown constant \( \dot{v} \).

To start with, note that the first two differential equation can be solved independently of \( \dot{a} \). In particular, we can draw a phase diagram in a \( h, c \) plane. Saddle-point stability applies under mild conditions (if downward sloping, the \( C=0 \) locus should be less steep than the \( \dot{h}_x=0 \) locus, which is violated only for very small values of \( \rho \)). Two possibilities arise because of the ambiguous sign of \( a_{21} \). If \( \alpha \) is large, \( a_{21} \) is negative, implying that the \( C=0 \) locus and the stable manifold slope upward (a sufficient condition is \( \alpha>\epsilon-1 \)). If \( \alpha \) is small, the \( C=0 \) locus and the stable manifold slope downward.

Ignoring the third differential equation, we can solve \( \dot{h}_x \) and \( C \) as a function of time \( t \), the unknown constant \( \dot{v} \), and the given shocks to the system \( \dot{h}_x^0, \dot{h}_y, \) and \( \dot{h}_y^s \), where \( \dot{h}_x^0 \) is the predetermined value for \( \dot{h}_x \) on time zero. Denoting the vector of these shocks by \( \dot{z} \), and the stable (negative) root by \( \lambda \), we can express the solutions as:

\[
\begin{align*}
\dot{h}_x &= \dot{h}_x(t, \dot{v}, \dot{z}) = e^{\lambda t} \dot{h}_x^0 + (1-e^{\lambda t}) \dot{h}_x(\infty, \dot{v}, \dot{z}) \\
C &= C(t, \dot{v}, \dot{z}) = e^{\lambda t} C(0, \dot{v}, \dot{z}) + (1-e^{\lambda t}) C(\infty, \dot{v}, \dot{z})
\end{align*}

We now make explicit the dependence of solutions not only on \( t \) but also on the shocks \( \dot{z} \) and on \( \dot{v} \).

Next we have to solve for \( \dot{a} \) and \( \dot{v} \). To this end we use the third differential equation and two natural restrictions on the value of net foreign assets \( \dot{a} \). First, we impose the condition that the long-run value of \( a \) is finite. The country has to be solvent: an exploding foreign debt ("Ponzi-game", \( a \to -\infty \)) should be excluded. The transversality condition rules out an infinitely large net foreign asset position (\( a \to -\infty \)). Second, we impose that net foreign assets are a predetermined variable: \( \dot{a}(0, \dot{v}, \dot{z}) = \dot{a}^0 \), where \( \dot{a}^0 = 0 \).

The procedure is as follows. We substitute the solutions for \( \dot{h}_x \) and \( C \) in the third differential equation. The resulting differential equation in \( \dot{a} \) and the constants \( \dot{\mu}_y, \dot{h}_y \), and \( \dot{v} \) can be solved. Imposing the conditions that \( a \) is finite for \( t=\infty \) and that \( \dot{a}=0 \) for \( t=0 \), we find a relation between \( \dot{h}_x^0, \dot{\mu}_y, \dot{h}_y \), and \( \dot{v} \) which is the solution for \( \dot{v} \). To simplify notation, write the third differential equation in (10) as

\[
\dot{a} = (r-g)\dot{a} + \ddot{x}
\]
where
\[ \ddot{x} = \ddot{x}(t, \tilde{v}, \tilde{z}) = a_{31}h_x(t, \tilde{v}, \tilde{z}) + a_{32}\ddot{x}(t, \tilde{v}, \tilde{z}) + a_{3d}(\mu_{\tilde{y}} - h_{\tilde{v}}) + a_{30} \tilde{v}. \] (Ap.21)

Substituting the solutions for \( h_x \) and \( C \), we can write:
\[ \dot{a}(t, \tilde{v}, \tilde{z}) = (r - g) \cdot \dot{a}(t, \tilde{v}, \tilde{z}) + e^{\lambda t} \left[ \ddot{x}(0, \tilde{v}, \tilde{z}) - \ddot{x}(\infty, \tilde{v}, \tilde{z}) \right] + \ddot{x}(\infty, \tilde{v}, \tilde{z}) \] . (Ap.22)

Integrating and imposing the no-Ponzi game condition, we arrive at:
\[ \dot{a}(t, \tilde{v}, \tilde{z}) = \left[ \frac{\ddot{x}(\infty, \tilde{v}, \tilde{z}) - \ddot{x}(0, \tilde{v}, \tilde{z})}{r - g - \lambda} \right] e^{\lambda t} + \left[ \frac{-\ddot{x}(\infty, \tilde{v}, \tilde{z})}{r - g} \right] (1 - e^{\lambda t}) \] . (Ap.23)

The terms in the first brackets equals \( \ddot{a}(0, \tilde{v}, \tilde{z}) \) which should equal to zero. From this equality, \( \tilde{v} \) is solved in terms of the vector of exogenous shocks \( \tilde{z} \).

The lower panel in figures 2 and 3 in the main text is found in the following way. First, find the relation between \( C \) and \( h_x \) along the stable manifold by substituting \( \dot{C}(t, \tilde{v}, \tilde{z}) = \lambda \left[ \dot{C}(t, \tilde{v}, \tilde{z}) - \dot{C}(\infty, \tilde{v}, \tilde{z}) \right] \) into the second differential equation. Next, substitute the resulting expression and the relation \( \dot{a} = -\lambda \dot{a}(\infty, \tilde{v}, \tilde{z}) \) in the third differential equation. This gives an expression for \( \ddot{a}(t, \tilde{v}, \tilde{z}) \) as the sum of a term multiplied by \( h_x \) and a term involving constants. With \( \ddot{a}(0, \tilde{v}, \tilde{z})=0 \), this constant should be zero (in fact this is an alternative way to find \( \tilde{v} \)). The term premultiplying \( h_x \) is the slope of the stable manifold depicting the relation between \( a \) and \( h_x \). We find this slope to be equal to \( \frac{(a_{21}a_{32} - a_{22}a_{31} + \lambda a_{31})}{(\lambda - a_{22})(\lambda - (r - g))} \), which is most likely to be negative.

**Appendix VI. Welfare**

Welfare at time \( t=0 \) [see (A.1)] can be written as:
\[ W(t) = \left( \frac{1}{1 - \rho} \right) C(t)^{1 - \rho} \int_{t}^{\infty} e^{-R(s)} ds , \]
where \( R \) is the cumulative growth-corrected discount rate, defined as:
\[ R(s) = \int_{0}^{s} \left[ \beta + (\rho - 1) \cdot \dot{C}(\tau) \right] d\tau . \]

Hence, welfare depends on the time path of consumption, captured by \( C(t) \) and \( C \). Taking total differentials, solving the resulting integrals by using the fact that all variables develop monotonically with speed of adjustment \( \lambda \) [see (Ap.20)], and taking into account that consumption grows at rate \( \sigma g \) in the steady state, we derive for welfare at \( t=0 \):
\[
\left( \frac{1}{1-\rho} \right) \frac{dW(t)}{W(t)} = \tilde{W}(t) = \tilde{C}(t) + \left( \frac{\lambda}{\theta + (\rho - 1)\alpha g - \lambda} \right) [\tilde{C}(t) - \tilde{C}(\infty)] .
\]

\( W \) is defined as \( W \equiv \frac{dW}{(1-\rho)W} \) so that \( W > 0 \) if welfare rises [note that \( W < (>) 0 \) if \( \rho > (<) 1 \)].
Preferences:
\[ U = \int_0^\infty (1 - p)^{\gamma-1} C(\gamma)^{1-\sigma} \exp(-\theta t) \, dt \]  \quad (A.1)

\[ C = X_c^\sigma Y_c^{1-\sigma}, \quad 0 < \sigma < 1 \]  \quad (A.2)

\[ X_c = \left( \sum_{i=1}^N \frac{e-1}{e} x_{ci} + \sum_{j=1}^n \frac{\alpha}{\mu} \frac{e-1}{e} \right) \frac{e}{e-1}, \quad \varepsilon > 1 \]  \quad (A.3)

Technology:
\[ Y = h_Y L_Y, \]  \quad (A.4)

\[ x_i = h_{xi} L_{xi}^\gamma Y_{xi}^{1-\gamma}, \]  \quad (A.5)

\[ h_{xi} = \xi \left( h_{xi}^{1-\alpha_{x_i}} h_{x_i}^{\alpha_{x_i}} H_{x_i}^{\alpha_{x_i}} H_{x_i}^{1-\alpha_{x_i}} \right) L_{ni}, \]  \quad (A.6)

Resource constraints:
\[ L_Y + \sum_{i=1}^N (L_{xi} + L_{ni}) = L, \]  \quad (A.7)

\[ Y_c + \sum_{i=1}^N Y_{xi} = Y, \]  \quad (A.8)

\[ x_{ci} + n x_{ci} = x_i, \]  \quad (A.9)

\[ \sum_{i=1}^N (x_i - x_{ci}) p_{xi} - \sum_{j=1}^n x_{cj} p_{sj} = \{ 0 \} \]  \quad (A.10)

---

<table>
<thead>
<tr>
<th>bars</th>
<th>denote a foreign variable.</th>
<th>preferences:</th>
</tr>
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<tbody>
<tr>
<td>$Y_c$</td>
<td>non-tradable consumption</td>
<td>$C$</td>
</tr>
<tr>
<td>$X_c$</td>
<td>tradable high-tech consumption index</td>
<td></td>
</tr>
<tr>
<td>$x_{ci}$</td>
<td>domestic production of tradable good $i$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>that is consumed domestically</td>
<td></td>
</tr>
<tr>
<td>$n$</td>
<td>number of firms in a country</td>
<td></td>
</tr>
<tr>
<td>$N$</td>
<td>number of countries in ROW</td>
<td></td>
</tr>
<tr>
<td>$Y$</td>
<td>total domestic non-tradables production,</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$x_i$ total domestic production of tradable good $i$</td>
<td></td>
</tr>
<tr>
<td>$L_{xi}$</td>
<td>labour allocated in sector $k$, firm $i$</td>
<td></td>
</tr>
<tr>
<td>$h_{xi}$</td>
<td>labour productivity in sector $k$, firm $i$</td>
<td></td>
</tr>
<tr>
<td>$H$</td>
<td>average labour productivity in national high-tech sector.</td>
<td></td>
</tr>
<tr>
<td>$L$</td>
<td>labour supply</td>
<td></td>
</tr>
<tr>
<td>$x_{cj}$</td>
<td>exports of tradable good $i$</td>
<td></td>
</tr>
<tr>
<td>$A$</td>
<td>Net foreign assets</td>
<td></td>
</tr>
</tbody>
</table>

Table A. Structure of the model
Maximization of consumer preferences (A.1), (A.2), and (A.3) subject to, respectively:

\[ \dot{F}(t) = r(t)F(t) + w(t)L - C(t)P_C(t) \]  \hspace{1cm} (B.1)

\[ X_cP_X + Y_cP_Y = CP_C \]  \hspace{1cm} (B.2)

\[ X_cP_X = \sum_{i=1}^{N} x_clP_{xi} + \sum_{j=1}^{n} \bar{x}_{ij}P_{xj} \]  \hspace{1cm} (B.3)

yields:

\[ \dot{C}/C = (1/\rho)(r - \dot{P}_C/P_C - \theta) \]  \hspace{1cm} (B.4)

\[ Y_cP_Y = (1-\sigma)CP_C \]  \hspace{1cm} (B.5)

\[ x_{ci} = X_c \left( \frac{p_{xi}}{P_X} \right)^{-\varepsilon} \]  \hspace{1cm} (B.6)

\[ \bar{x}_{ij} = X_c \left( \frac{p_{yj}}{P_X} \right)^{-\varepsilon} \]  \hspace{1cm} (B.7)

where

\[ P_C = \left( \frac{P_C}{P_C} \right)^{\sigma} \left( \frac{P_Y}{(1-\sigma)} \right)^{1-\sigma} \]  \hspace{1cm} (B.8)

\[ P_X = \left( \frac{\sum_{i=1}^{N} p_{xi}^{1-\varepsilon} + \sum_{j=1}^{n} \bar{p}_{yj}^{1-\varepsilon}}{1/(1-\varepsilon)} \right) \]  \hspace{1cm} (B.9)

\[ P_c, P_X \]  price indices of consumption and tradables respectively.

\[ p_{yi}, p_{yo} \]  prices of non-tradables, home-produced tradables and imports respectively.

\[ w, r \]  wage and interest rate respectively

Table B. Consumer behaviour
X-sector:  

\[
V_i = \int_0^\infty \left[ x_i(t) p_{x_i}(t) - Y_{x_i}(t) p_{x_i}(t) - \left( L_{x_i}(t) + L_{y_i}(t) \right) w(t) \right] \exp(-\int_0^t r(s)ds)dt
\]

(C.1)

\[
x_i = X_c \left( p_{x_i}/P_X \right)^\varepsilon + n X_c \left( p_{x_i}/P_X \right)^{\varepsilon - \delta} = \Omega \ p_{x_i}^{-\varepsilon}
\]

(C.2)

maximization of (C.1) w.r.t. \( p_{x_i}, Y_{x_i} \) and \( L_{r_i} \), s.t. (A.5), (A.6) and (C.2) yields

\[
p_{x_i} = \left( \mu_{x_i}/h_{x_i} \right) \ (w/\gamma)' \left( p_{x_i}/(1-\gamma) \right)^{1-\gamma}
\]

(C.3)

\[
p_{y_i}Y_{x_i}/wL_{x_i} = (1-\gamma)/\gamma
\]

(C.4)

\[
p_{hi} = w / \xi K_i
\]

(C.5)

\[
\left( p_{x_i}/\mu_{X_i} \right) \left( x_i/h_{x_i} \right) + p_{hi}^e \left( 1 - \alpha_h - \alpha_p \right) (K_i/h_{x_i})L_{r_i} + \dot{p}_{hi} = r \ p_{hi}
\]

(C.6)

where

\[
K_i = h_{x_i}^{1-s_y-s_f} H^{h_{x_i}} \sum_i H^{s_f}
\]

\[
\mu_{X_i} = e/(e-1)
\]

Y-sector:

\[
p_{y_i} = \mu_{y_i} w/h_{y_i}
\]

(C.7)

where  \( \mu_{y_i} = m/(m-1) \)

---

\( K_i \)  
firm \( i \)'s knowledge base in R&D

\( \mu_{hi} \)  
mrk-up rate in sector \( k \).

\( m \)  
number of firms in Y-sector.

---

Table C. Producer behaviour
Consumption decision (Ramsey):
\[ r = \bar{\sigma} + (\alpha \sigma + 1 - \sigma) \bar{g} = \bar{r}. \] (D.1)

Investment decision:
\[ \xi(h_s^i/\bar{h}_s)^{-\alpha_r} L_s/\gamma = r - (1 - \alpha_h - \alpha_r) \bar{g}. \] (D.2)

Labour market equilibrium:
\[ \bar{g} = \xi(h_s^i/\bar{h}_s)^{-\alpha_r} \left[ \frac{L}{N} - \frac{Y_c}{h_p N} - \left( \frac{1 - \gamma + \gamma \mu_r}{\mu_r} \right) \frac{L_s}{\gamma} \right]. \] (D.3)

Equilibrium in the market for non-tradables:
\[ Y_c = (1 - \sigma)(h_p/\mu_r) CP_c/w. \] (D.4)

Balance of payments equilibrium:
\[ \mu_x NL_x/\gamma - \sigma CP_c/w = - (\bar{r} - \bar{g}) A/w. \] (D.5)

Balance of payments regime:
\[ A = 0 \text{ (balanced trade) or } A \neq 0 \text{ (perfect capital mobility)} \] (D.6)

Table D. Key relationships in the steady state
Consumption decision (Ramsey):

\[ \hat{C} = \frac{1}{\rho} \left[ r^* - (1-\sigma)\hat{h}_x + \left( \frac{1-\sigma}{\epsilon} \right) (\hat{L}_x + \hat{h}_x) \right]. \] (E.1)

Investment decision:

\[ r^* = (\zeta L_x/Y) \left[ \bar{L}_x - \alpha \hat{h}_x \right] + \left( 1-\alpha \right) \hat{h}_x - \left( 1/\epsilon \right) \left( \hat{L}_x + \hat{h}_x \right). \] (E.2)

Labour market equilibrium:

\[ \hat{h}_x = - \left( \frac{\zeta Y_x}{h_xN} \right) \left( \bar{Y}_c - \bar{h}_y \right) - \left( \frac{\zeta L_x}{\gamma} \right) \left( \frac{1-\gamma+\gamma \mu_y}{\mu_y} \right) \hat{L}_x + \left( \frac{\zeta L_x}{\gamma} \right) \left( \frac{1-\gamma}{\mu_y} \right) \bar{h}_y - (\alpha g) \hat{h}_x. \] (E.3)

Equilibrium in the (world) market for tradables:

\[ \hat{p}_x = \frac{1-\gamma}{\epsilon} (\mu_y - \bar{h}_y) - \frac{1}{\epsilon} (\hat{h}_x + \bar{L}_x). \] (E.4)

Equilibrium in the market for non-tradables:

\[ \bar{Y}_c = \bar{C} - \sigma \left( \hat{h}_x - \frac{1}{\epsilon} (h_x + \bar{L}_x) \right) - \sigma \left( \gamma + \frac{1-\gamma}{\epsilon} \right) (\mu_y - \bar{h}_y). \] (E.5)

Balance of payments equilibrium:

\[ \hat{a} = (\bar{Y} - \bar{C})\hat{a} + \left( \frac{N x p_x}{h_x} \right) (1-\epsilon) \bar{p}_x - \left( \frac{\sigma CP_x}{h_x} \right) \left[ \bar{C} + (1-\sigma) \left( \bar{p}_x + \bar{h}_x + \bar{Y} (\mu_y - \bar{h}_y) \right) \right]. \] (E.6)

Balance of payments regime:

\[ \hat{a} = \bar{a} = 0 \) (balanced trade) or \( \rho = 0 \) (perfect capital mobility) \] (E.7)

Note: we have assumed \( s \sim 0 \) (small country assumption) and defined \( \zeta = \xi \left( h_x/\bar{h}_x \right)^{-\alpha}. \)

Table E. Key relationships in linearized form
<table>
<thead>
<tr>
<th>Case</th>
<th>Balanced Trade</th>
<th>Capital Mobility</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Period</td>
<td></td>
</tr>
<tr>
<td>Variable</td>
<td>t = 0</td>
<td>t → ∞</td>
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<tr>
<td>Price tradables</td>
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<td>Productivity</td>
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<td>Growth rate</td>
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<td>Consumption</td>
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<td>-</td>
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Rate of convergence (%) 1.596 2.109

Table 1. Catching-up $\bar{h}_x(0)=−1$
<table>
<thead>
<tr>
<th>Variable</th>
<th>Balanced Trade</th>
<th>Capital Mobility</th>
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<tr>
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</tr>
<tr>
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<td>Rate of convergence (%)</td>
<td>1.596</td>
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</table>

Table 2. Increasing regulation ($\mu_i=1$)
Consumption decision (Ramsey):

\[ \hat{c} = \frac{1}{\rho} \left[ r - (1-\sigma)\hat{h}_x + \left( \frac{1-\sigma}{e} \right) \left( \hat{L}_x + \hat{x} - \hat{x} \right) - \theta \right]. \] (F.1)

Investment decision:

\[ r = \xi \left( \frac{h_x}{\hat{h}_x} \right)^{e} \frac{L_x}{Y} + (1-\alpha)\hat{h}_z - \alpha \bar{g} + (\bar{g} - \hat{h}_z - \bar{L}_s)/e. \] (F.2)

Labour market equilibrium:

\[ \hat{h}_x = \xi \left( \frac{h_x}{\hat{h}_x} \right)^{e} \left[ \frac{L}{N} - \frac{Y_c}{h_x N} - \left( \frac{1-\gamma + \gamma \mu_y}{\mu_y} \right) \frac{L_x}{Y} \right]. \] (F.3)

Equilibrium in the (world) market for tradables:

\[ p_x = \left( \frac{\hat{h}_x L_x}{h_x L_x} \right)^{1/e} \left( \frac{\mu_y}{\mu_y} \right)^{(1-\gamma)e}. \] (F.4)

Equilibrium in the market for non-tradables:

\[ Y_c = (1-\sigma)(h_x/\mu_y)CP_C/w. \] (F.5)

Balance of payments equilibrium:

\[ \mu_x w \gamma L_x = \sigma CP_C = \dot{A} - \bar{\gamma} \dot{A}. \] (F.6)

Balance of payments regime:

\[ \dot{A} = \dot{A} = 0 \text{ (balanced trade) or } r = \bar{r} \text{ (perfect capital mobility)} \] (F.7)

Table F. Key relationships
Figure 3. Increase in $\mu_y$. 
Figure 2. Capital mobility, large $\alpha_f$ (left panel) and small $\alpha_f$ (right panel).
Figure 4: Welfare effects of deregulation